

Study of the nuclear deformation in relativistic isobar collisions at RHIC

Chunjian Zhang

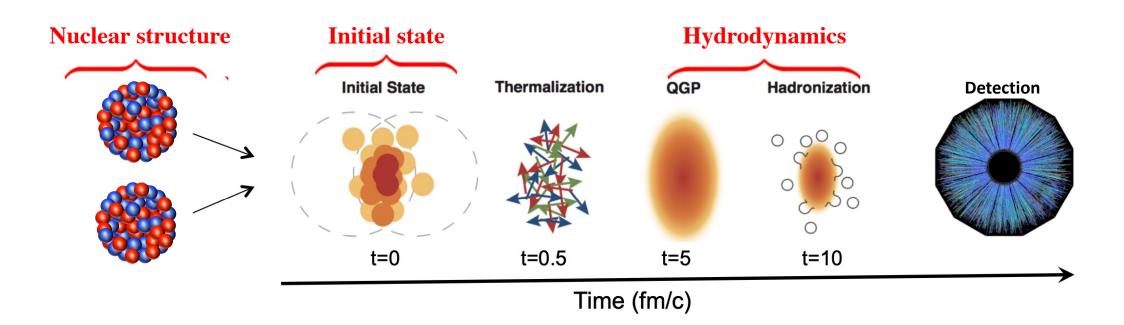
For the STAR Collaboration







Heavy-ion collisions and nuclear structure



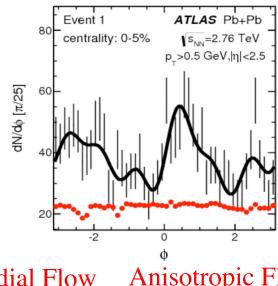
Space-time evolution of heavy-ion collisions can be considered as a hydrodynamic response to the nucleon density distribution in the initial overlap region in the transverse plane, driven by pressure gradient.

The shape and the size of the overlap are controlled by the shape and radial profile of the colliding nuclei.

Hydrodynamic response to initial state

Nuclear Structure Initial State centrality: 0-5% dN/dφ [π/25] **Imaging?** hydrodynamic response $\frac{1+e^{\left(r-R_0\left(1+\sum_noldsymbol{eta}_n^{N}Y_n^0(heta,\phi) ight)\right)/\mathbf{a_0}}}$ **Initial Size Initial Shape** Radial Flow $R_\perp^2 \propto \left\langle r_\perp^2 ight angle$ $\mathcal{E}_n \propto \langle r_\perp^n e^{in\phi} angle$

Produced Particle Flow



Anisotropic Flow

$$rac{d^2N}{d\phi dp_T} = rac{N(p_T)}{\left(\sum_n rac{V_{
m n}}{v_{
m n}}e^{-in\phi}
ight)}$$

D. Teaney et al., arXiv:1206.1905

Approximate linear response in each event:

 R_0

 β_2 • Quadrupole deformation

 β_3 \rightarrow Octupole deformation

 $a_0 \rightarrow$ Surface diffuseness

→ Nuclear size

$$rac{\delta[p_T]}{[p_T]} \propto -rac{\delta R_\perp}{R_\perp}$$

$$V_n \propto \mathcal{E}_n$$

Connecting shape ε_n and size R to β_n

• ε_n is related to the shape of the Y_n^n projected to the transverse plane

$$\mathcal{E}_n = -rac{\left\langle r_\perp^n e^{in\phi}
ight
angle}{\left\langle r_\perp^n
ight
angle} \propto \ \left\langle Y_n^n
ight
angle = oldsymbol{\epsilon}_{n;0} + oldsymbol{p}_n(\Omega_1,\Omega_2)eta_n + \mathcal{O}ig(eta_n^2ig)$$
 Undeformed Phase factor

J. Jia, arXiv:2109.00604

 Y_n^n : spherical harmonics

Flow variance
$$\left\langle \boldsymbol{v}_{n}^{2} \right\rangle \propto \left\langle \varepsilon_{n}^{2} \right\rangle = \left\langle \varepsilon_{0}^{2} \right\rangle + \left\langle \boldsymbol{p}_{2}(\Omega_{1},\Omega_{2})\boldsymbol{p}_{2}^{*}(\Omega_{1},\Omega_{2}) \right\rangle \beta_{n}^{2}$$

• R_{\perp} is related to Y_2^0 projected to the transverse plane

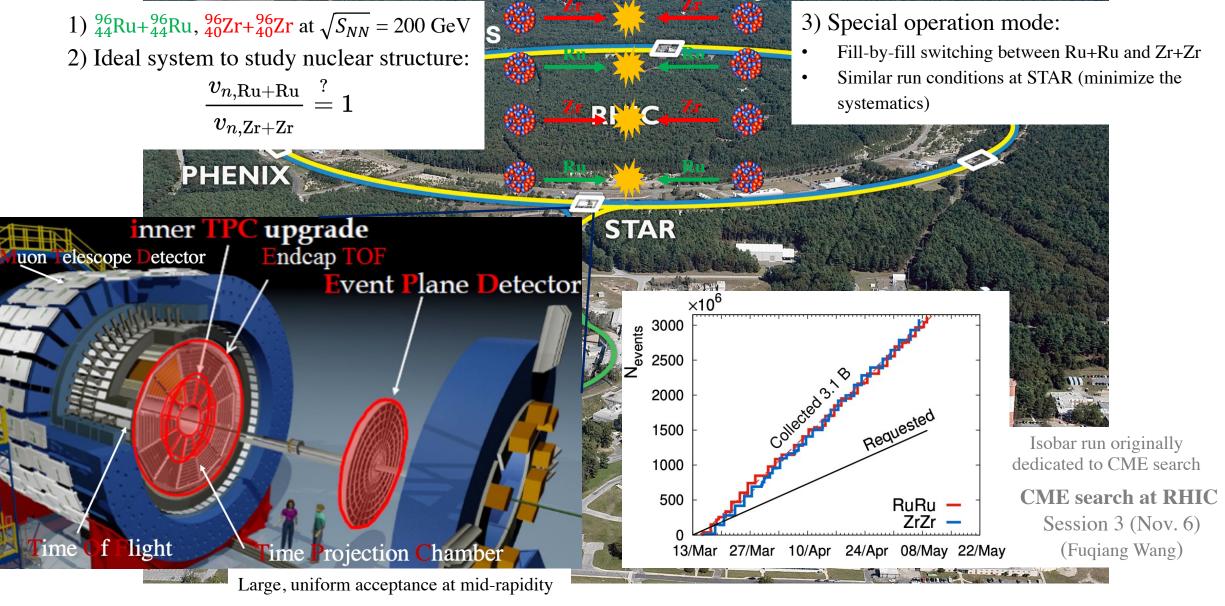
$$R_{\perp}^2 = \left\langle x^2
ight
angle + \left\langle y^2
ight
angle \propto \left\langle 1 - 2 \sqrt{rac{\pi}{5}} Y_2^0
ight
angle \hspace{1.5cm} d_{\perp} \equiv 1/R_{\perp}$$

$$rac{\delta d_{\perp}}{d_{\perp}} = \delta_d + p_0(\Omega_1,\Omega_2)eta_2 + \mathcal{O}ig(eta_2^2ig)$$

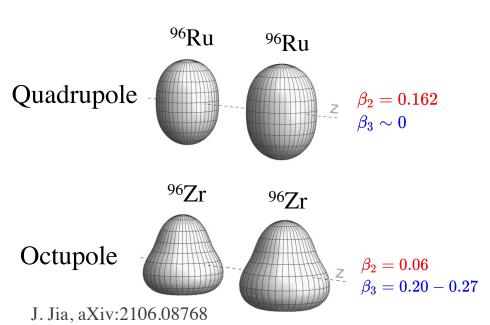
fluctuation of δ_d (ϵ_0) is uncorrelated with p_0 (\boldsymbol{p}_2)

Variance
$$\left\langle \left(\delta[p_{\mathrm{T}}]/[p_{\mathrm{T}}] \right)^2 \right\rangle \propto \left\langle \left(\delta d_{\perp}/d_{\perp} \right)^2 \right\rangle = \left\langle \delta_d^2 \right\rangle + \left\langle p_0(\Omega_1,\Omega_2)^2 \right\rangle \beta_2^2$$

The STAR detector and unique isobar run



Nuclear deformation in isobar collisions

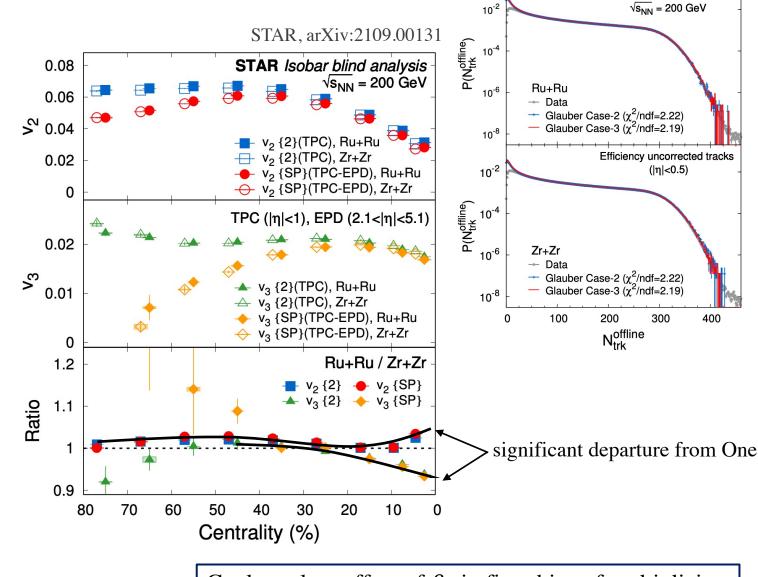


Nuclear structure data on Ru/Zr deformation:

	eta_2 .	$E_{2_1^+}$ (MeV)	eta_3 1	$\Xi_{3_1^-}$ (MeV)
	0.154	0.83	-	3.08
$^{96}\mathrm{Zr}$	0.062	1.75	0.202,0.235,0.27	1.90
eta_2	$=rac{4\pi}{3ZR_0^2}$	$-\sqrt{rac{B(E2)\uparrow}{\mathrm{e}^2}}$	$eta_3 = rac{4\pi}{3ZR_0^3}\sqrt{rac{B(E)}{e}}$	[2] [2] [2] [3]

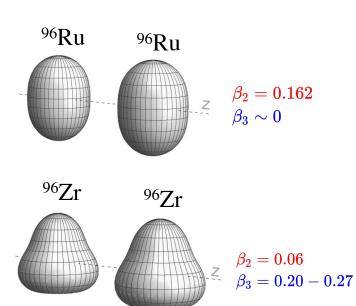
C. Zhang et al., arXiv:2109.01631

G. Giacalone et al., arXiv:2102.08158



Goal: explore effect of β_n in finer bins of multiplicity

STAR Isobar blind analysis



J. Jia, aXiv:2106.08768

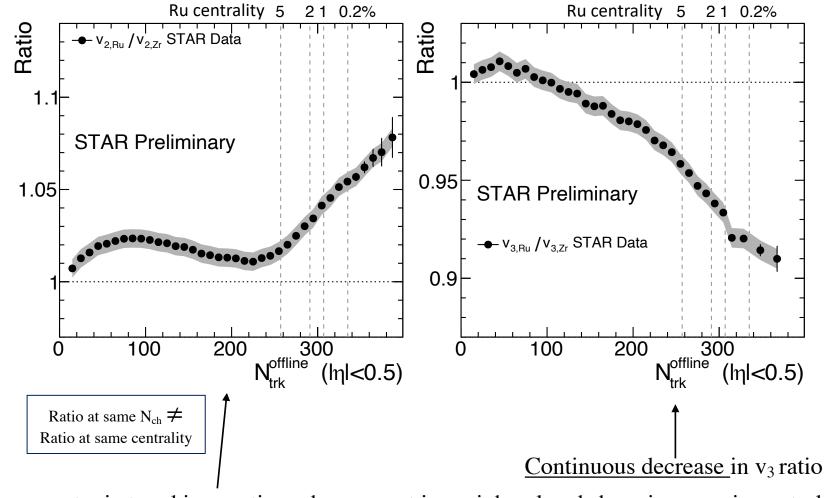
Heavy-ion expectation:

$$v_2^2 = a_2 + b_2 eta_2^2 + b_{2,3} eta_3^2, \quad v_3^2 = a_3 + b_3 eta_3^2$$

$$rac{v_{2, ext{Ru}}^2}{v_{2, ext{Zr}}^2}pprox 1+rac{b_2}{a_2}ig(eta_{2, ext{Ru}}^2-eta_{2, ext{Zr}}^2ig)-rac{b_{2,3}}{a_2}eta_{3, ext{Zr}}^2$$

$$rac{v_{3, ext{Ru}}^2}{v_{3, ext{Zr}}^2}pprox 1-rac{b_3}{a_3}eta_{3, ext{Zr}}^2<1$$
 Cancelation expected in non-central collisions

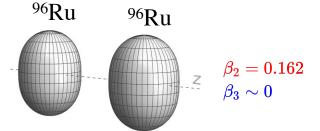
v_2 and v_3 ratio

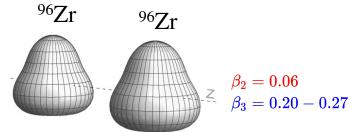


Nonmonotonic trend in v₂ ratio: enhancement in peripheral and sharp increase in central

✓ The large differences of v_2 and v_3 suggest $\beta_{2,Ru} \gg \beta_{2,Zr}$ and $\beta_{3,Ru} \ll \beta_{3,Zr}$.

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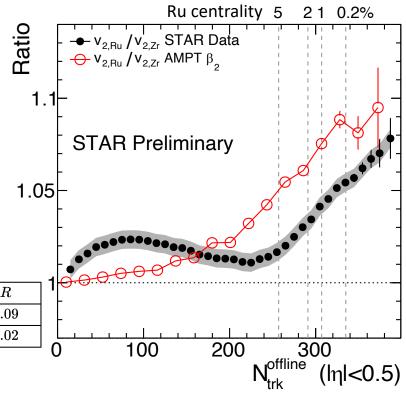
Species	eta_2	eta_3	a_0	R
Ru+Ru	0.162	0.00	0.46	5.09
m Zr + Zr	0.06	0.20	0.52	5.02

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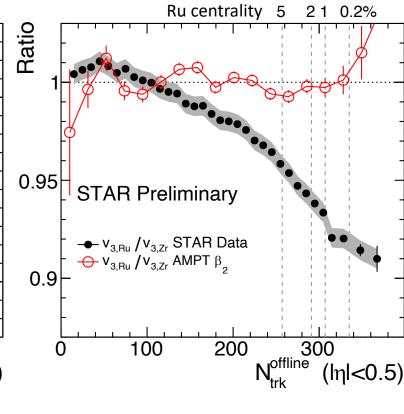
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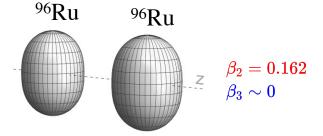


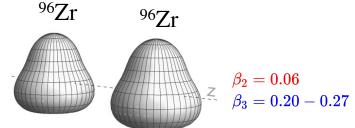
 v_2 ratio: large increase from $\beta_{2,Ru}$ in central



 v_3 ratio: not affected by $\beta_{2,Ru}$

C. Zhang et al., arXiv:2109.01631; G. Giacalone et al., 2105.01638





J. Jia, aXiv:2	106.08768
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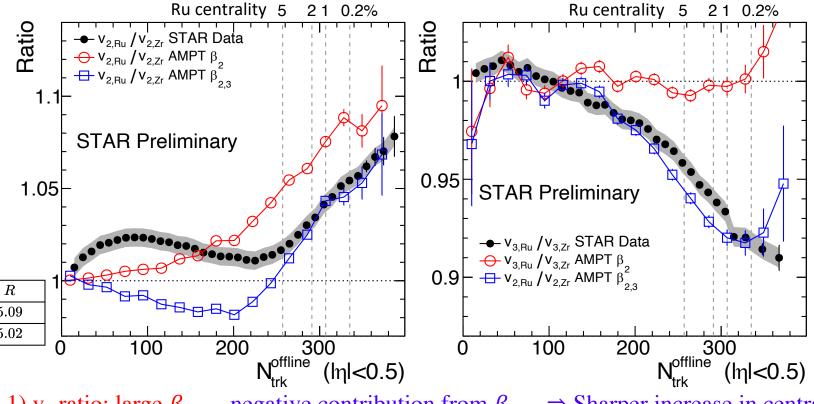
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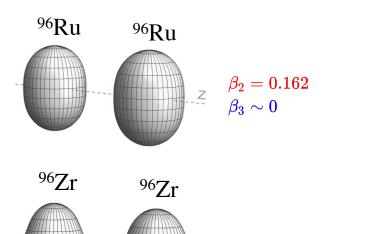
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 Cancelation expected in non-central collisions



- 1) v_2 ratio: large $\beta_{2,Ru}$, negative contribution from $\beta_{3,Zr} \Rightarrow$ Sharper increase in central
- 2) v_3 ratio: strong decrease from $\beta_{3,Zr}$ with negligible $\beta_{2,Ru}$ distortion

- ✓ The large differences of v_2 and v_3 suggest $\beta_{2,Ru} \gg \beta_{2,Zr}$ and $\beta_{3,Ru} \ll \beta_{3,Zr}$.
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 $\beta_2 = 0.06$

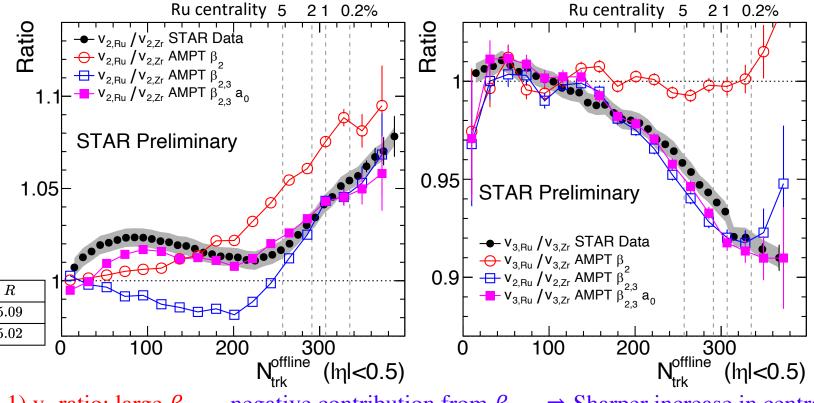
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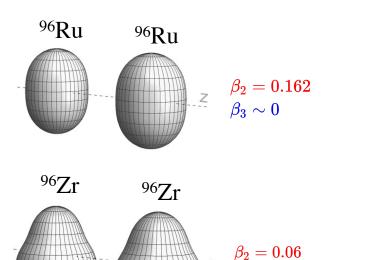
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Direct indication of octupole deformation in heavy-ion collisions.

H. Xu et al., arXiv:1808.06711, 2103.05595, 1910.06170

C. Zhang et al., arXiv:2109.01631; G. Giacalone et al., 2105.01638

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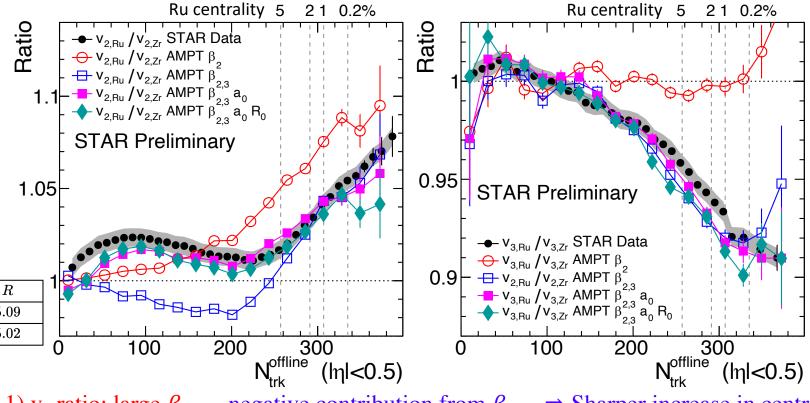
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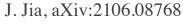
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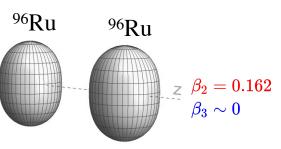


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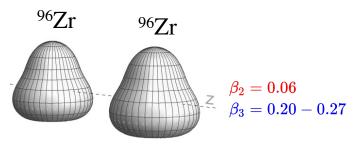


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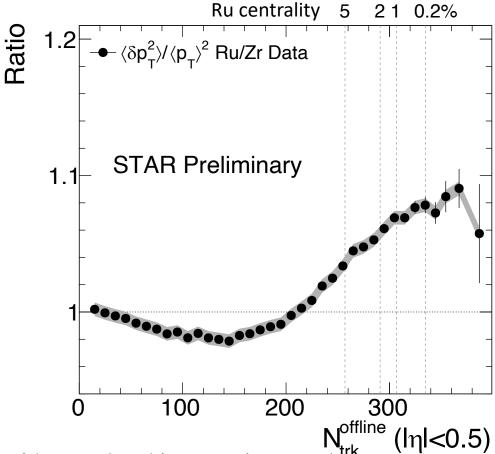
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ight)^{2}
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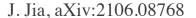


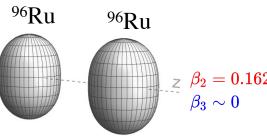
$$\left\langle \left(\delta[p_{
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ight
angle \propto \left\langle \left(\delta d_{\perp}/d_{\perp}
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ight
angle = \left\langle \delta_d^2
ight
angle + \left\langle p_0(\Omega_1,\Omega_2,\gamma)^2
ight
angle eta_2^2$$



1) Nonmonotonic trend: large suppression in mid-central and increase in central

Ratio





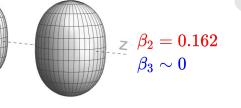
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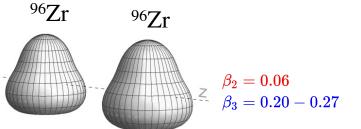
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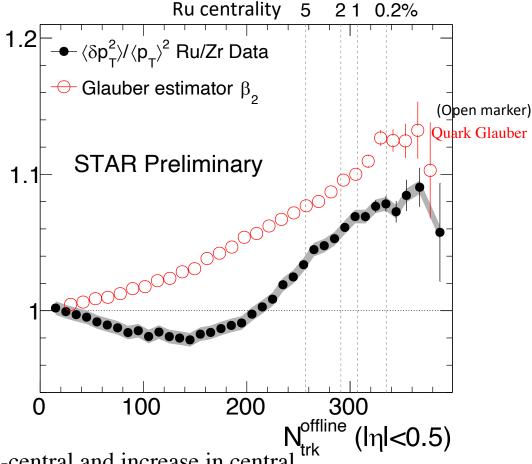
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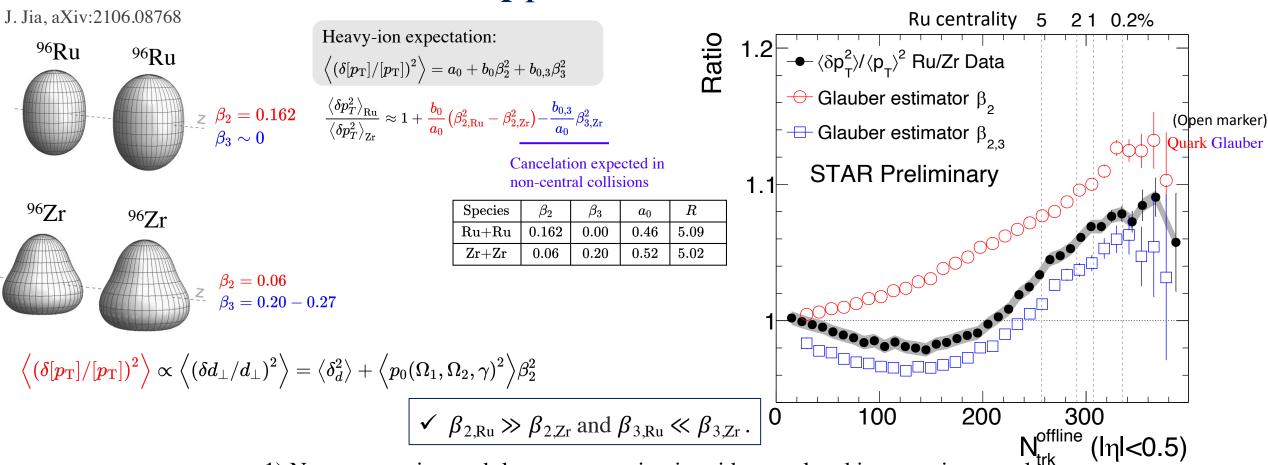




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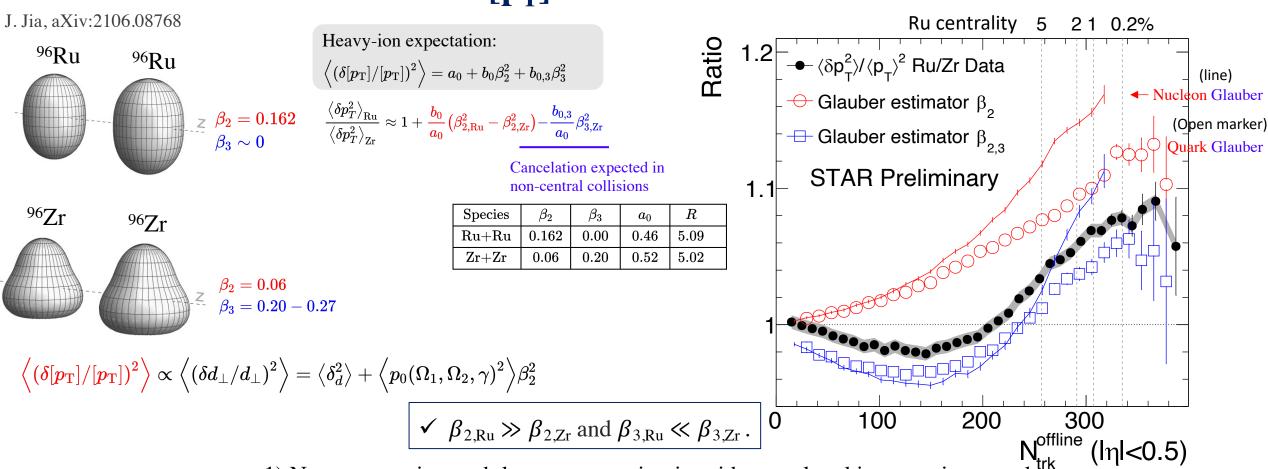


- 1) Nonmonotonic trend: large suppression in mid-central and increase in central
- 2) Enhancement from mid-central \Rightarrow large $\beta_{2,Ru}$



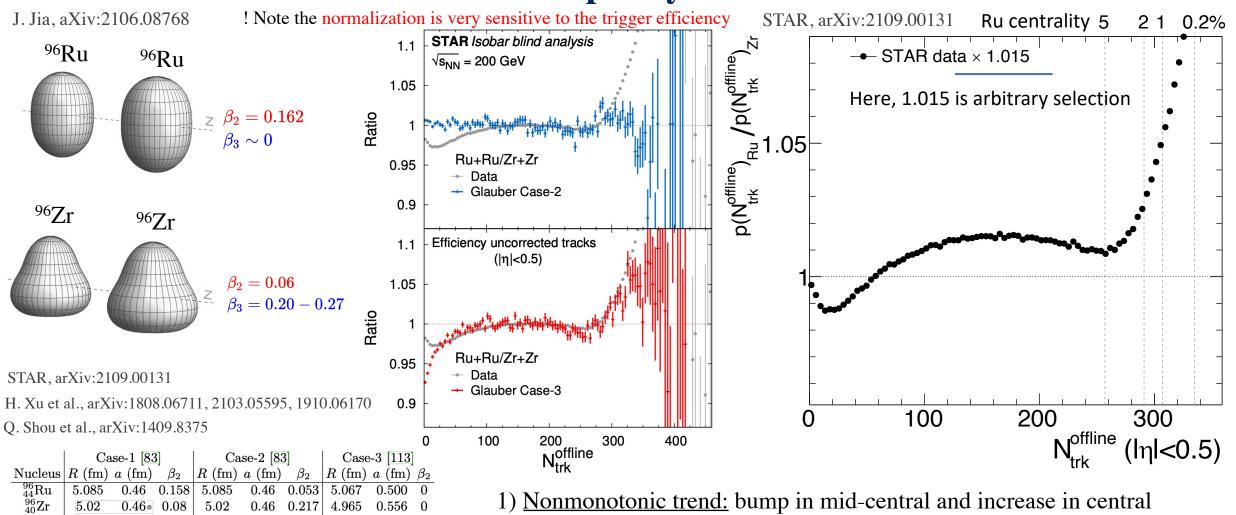
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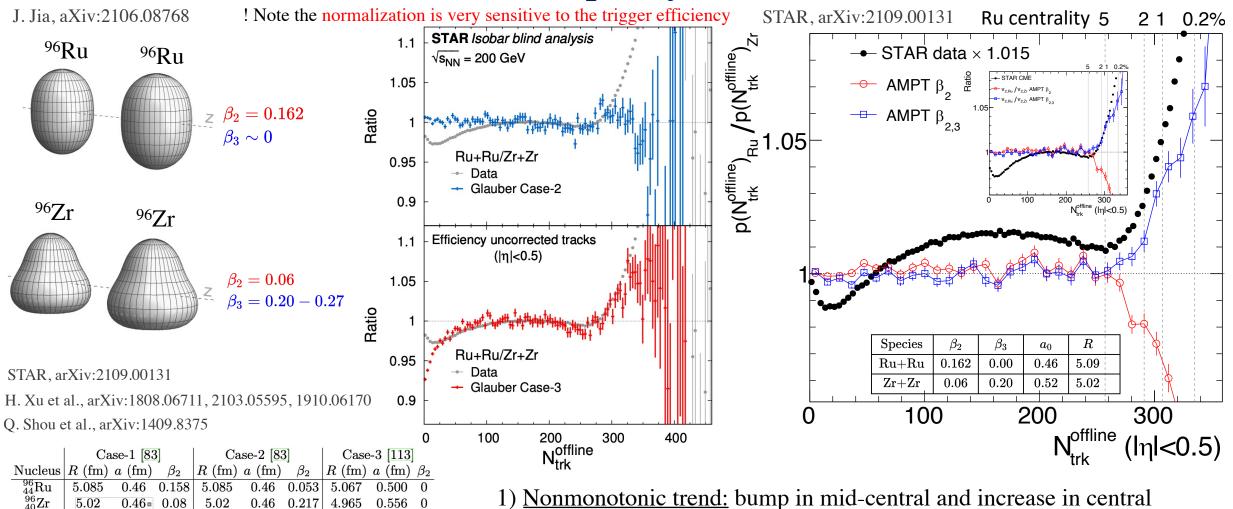
Variance of $[p_T]$ fluctuations can also be used to constrain the nuclear deformation.



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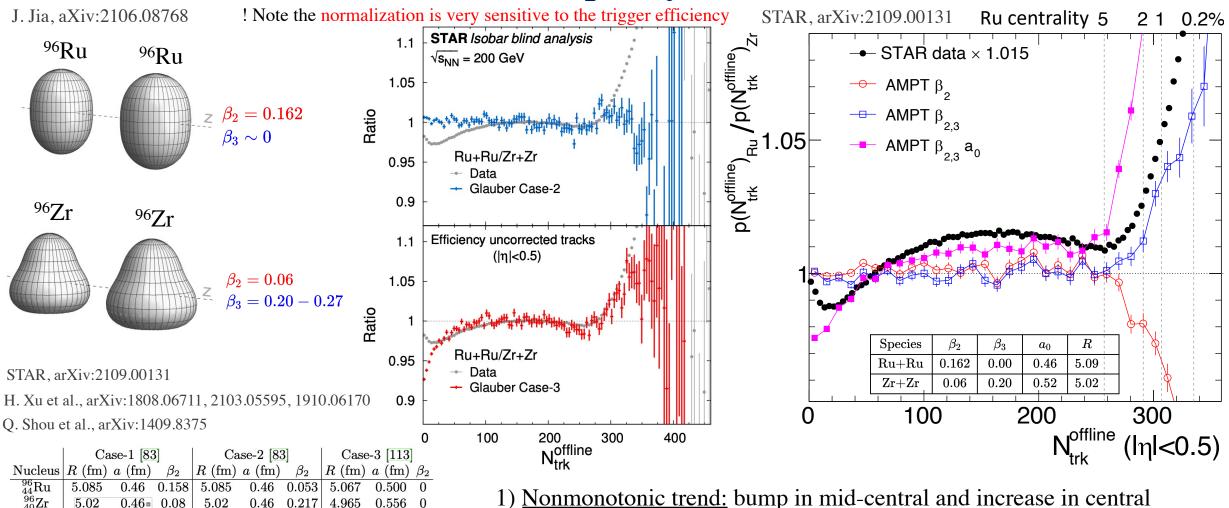
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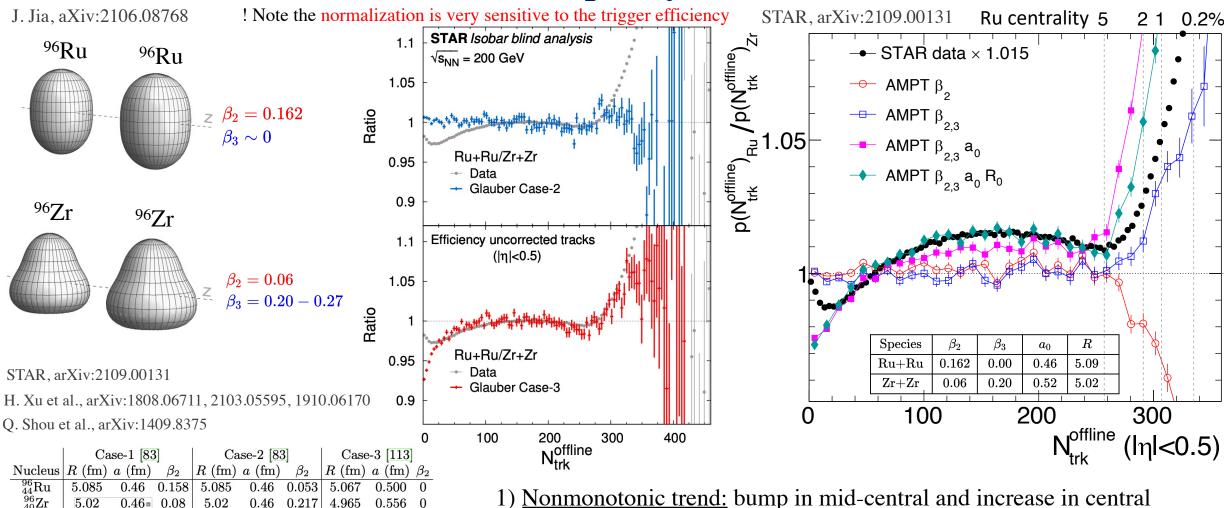


- 1) Nonmonotonic trend: bump in mid-central and increase in central 5.02 $0.46 \quad 0.217 \quad 4.965 \quad 0.556 \quad 0$
- 2) When only consider β_2 in case-1 and case-2: constant in peripheral and mid-central, but decrease in central.
- 3) But if you consider β_3 in Zr: also can almost get the same tail as Case-3.

5.02

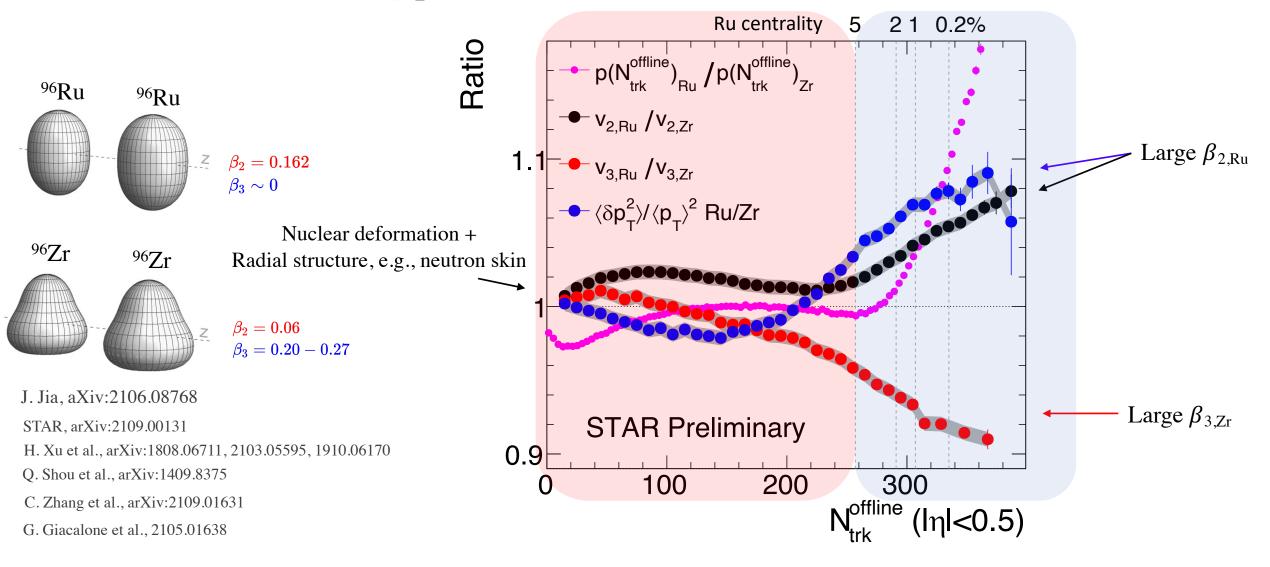


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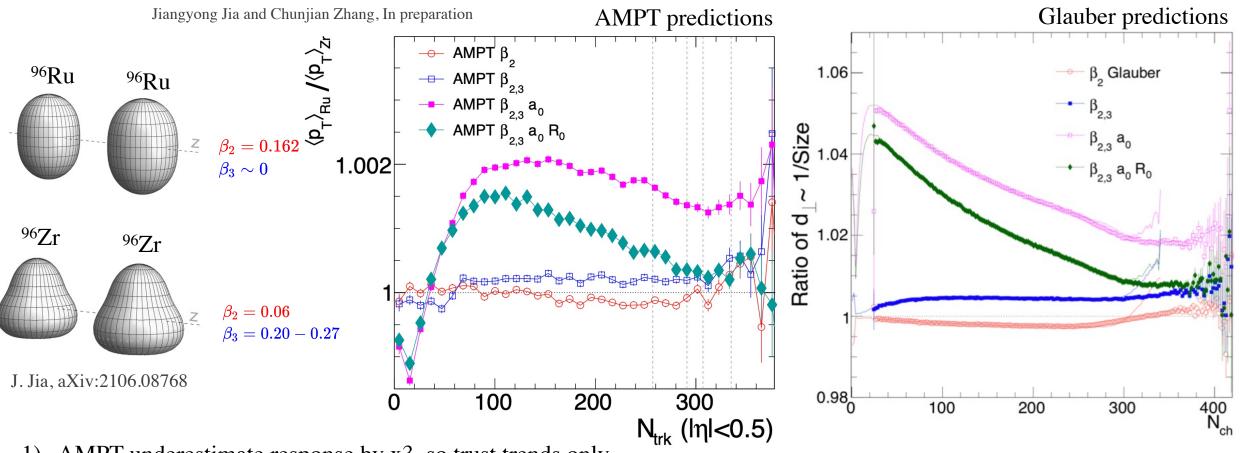
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- 5) Nuclear size R also can affect the trend.

flow, [p_T]-variance and multiplicity ratio



Ratio of any bulk observables can image the shape of the nuclei.

New proposed observable: Nuclear structure via $\langle p_T \rangle$



- 1) AMPT underestimate response by x3, so trust trends only.
- 2) β_2 , β_3 small impact in noncentral, but some increase in UCC
- 3) Enhancement dominated by surface diffuseness

- 4) Radius difference leads to stronger N_{ch} dependence
- 5) Glauber model also describe the trends.

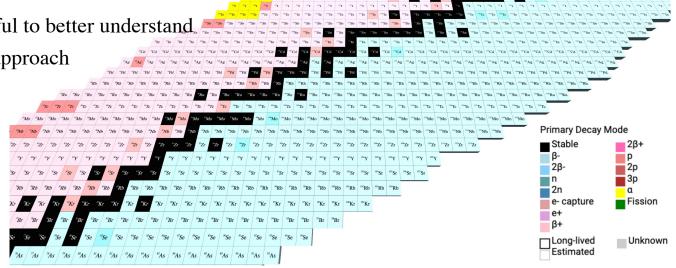
Ratio of $\langle p_T \rangle_{Ru/Zr}$ also could reflect the nuclear structure.

Conclusions and outlooks

- ✓ Isobar collisions are a new tool to study the nuclear structure.
- \checkmark The ratios of v_2 , v_3 , $\langle \delta p_T^2 \rangle$ and multiplicity have large deviation from one implying:

$$m{eta}_{2,\mathrm{Ru}}\gg m{eta}_{2,\mathrm{Zr}}, m{eta}_{3,\mathrm{Ru}}\ll m{eta}_{3,\mathrm{Zr}}$$
 and radial structure, e.g., neutron skin in $^{96}\mathrm{Zr}$

- ✓ This is the direct observation of 96 Zr octupole deformation/collectivity using heavy-ion collisions.
- ✓ Isobar collisions open up new opportunity to study nuclear structure at a very short time scale ($\sim 10^{-24}$ s) through heavy-ion collisions
 - By doing future deformed-system scan
 - Species with well known deformation will be useful to better understand, the systematics and establish the efficacy of this approach



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